

**PREHOMOGENEOUS SPACES ASSOCIATED WITH NILPOTENT
ORBITS IN TYPE EVI**

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Nilpotent orbits in type EVI				
Orbit	$K_{\mathbb{C}}$ diagram	i	$\dim \mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$	Highest weights of $\mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$
1.	 $\begin{array}{cccccc} & & \circ & 1 & & \\ & \circ & - & \circ & - & \circ & \circ \\ 0 & 0 & 0 & 0 & 0 & 1 \end{array}$	1	16	$(0, 1, 0, 0, 0, 0, 0)$ $(0, 0, 0, 0, 0, 0, 2)$
2.	 $\begin{array}{cccccc} & & \circ & 0 & & \\ & \circ & - & \circ & - & \circ & \circ \\ 0 & 1 & 0 & 0 & 0 & 2 \end{array}$	1	16	$(1, -1, 1, 0, 0, 0, 0)$
		2	2	$(0, 1, 0, 0, 0, 0, 0)$ $(0, 0, 0, 0, 0, 0, 2)$
3.	 $\begin{array}{cccccc} & & \circ & 0 & & \\ & \circ & - & \circ & - & \circ & \circ \\ 0 & 0 & 0 & 1 & 0 & 0 \end{array}$	1	16	$(1, 0, 0, -1, 1, 1, 0)$
		2	6	$(0, 1, 0, 0, 0, 0, 0)$
4.	 $\begin{array}{cccccc} & & \circ & 1 & & \\ & \circ & - & \circ & - & \circ & \circ \\ 0 & 0 & 0 & 0 & 0 & 3 \end{array}$	1	15	$(0, 1, 0, 0, 0, 0, 0)$
		3	1	$(0, 0, 0, 0, 0, 0, 2)$
5.	 $\begin{array}{cccccc} & & \circ & 1 & & \\ & \circ & - & \circ & - & \circ & \circ \\ 0 & 1 & 0 & 0 & 0 & 1 \end{array}$	1	15	$(0, -1, 0, 1, 0, 0, 0)$ $(1, 0, 0, 0, -1, 1, 0)$ $(0, 0, 0, 0, 0, 2)$
		2	8	$(1, -1, 1, 0, 0, 0, 0)$
		3	1	$(0, 1, 0, 0, 0, 0, 0)$
6.	 $\begin{array}{cccccc} & & \circ & 0 & & \\ & \circ & - & \circ & - & \circ & \circ \\ 0 & 0 & 0 & 0 & 0 & 4 \end{array}$	4	1	$(0, 0, 0, 0, 0, 0, 2)$
7.	 $\begin{array}{cccccc} & & \circ & 2 & & \\ & \circ & - & \circ & - & \circ & \circ \\ 0 & 0 & 0 & 0 & 0 & 2 \end{array}$	2	16	$(0, 1, 0, 0, 0, 0, 0)$ $(0, 0, 0, 0, 0, 0, 2)$
8.	 $\begin{array}{cccccc} & & \circ & 0 & & \\ & \circ & - & \circ & - & \circ & \circ \\ 0 & 2 & 0 & 0 & 0 & 0 \end{array}$	2	16	$(1, -1, 1, 0, 0, 0, 0)$
		4	1	$(0, 1, 0, 0, 0, 0, 0)$
9.	 $\begin{array}{cccccc} & & \circ & 0 & & \\ & \circ & - & \circ & - & \circ & \circ \\ 1 & 1 & 0 & 0 & 1 & 1 \end{array}$	1	12	$(2, -1, 0, 0, 0, 0, 0)$ $(-1, 1, 0, 0, 1, -1, 0)$ $(0, -1, 0, 1, 0, 0, 0)$ $(0, 0, 0, 0, 0, 0, 2)$
		2	8	$(1, 0, 0, 0, 1, -1, 0)$ $(-1, 0, 1, 0, 0, 0, 0)$
		<i>(continued on next page)</i>		

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Nilpotent orbits in type EVI (continued)				
Orbit	$K_{\mathbb{C}}$ diagram	i	$\dim \mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$	Highest weights of $\mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$
		3	4	(1, -1, 1, 0, 0, 0) (0, 1, 0, 0, 0, 0)
10.		1	12	(-1, 1, 0, -1, 1, 1, 0)
		2	6	(1, 0, 1, -1, 0, 0, 0) (-1, 0, 1, 0, 0, 0, 0)
		3	4	(1, 0, 0, -1, 1, 1, 0)
		4	3	(0, 1, 0, 0, 0, 0, 0)
11.		1	12	(1, 0, 1, -1, 0, 0, 0) (0, -1, 1, -1, 1, 1, 0)
		2	10	(0, -1, 0, 1, 0, 0, 0) (1, 0, 0, -1, 1, 1, 0) (0, 0, 0, 0, 0, 2)
		3	4	(1, -1, 1, 0, 0, 0, 0)
		4	1	(0, 1, 0, 0, 0, 0, 0)
12.		1	8	(1, 0, 0, 0, -1, 1, 0)
		2	6	(0, -1, 0, 1, 0, 0, 0)
		3	8	(1, -1, 1, 0, 0, 0, 0)
		4	2	(0, 1, 0, 0, 0, 0, 0) (0, 0, 0, 0, 0, 0, 2)
13.		1	8	(1, 0, 0, 0, -1, 1, 0)
		2	2	(0, 0, 0, -1, 2, 0, 0) (0, 0, 0, 0, 0, 0, 2)
		3	8	(1, 0, 0, -1, 1, 1, 0)
		4	6	(0, 1, 0, 0, 0, 0, 0)
14.		4	10	(0, 1, 0, 0, 0, 0, 0)
15.		2	16	(1, 0, 0, -1, 1, 1, 0)
		4	6	(0, 1, 0, 0, 0, 0, 0)
16.		1	10	(0, 0, 0, -1, 2, 0, 0) (0, -1, 1, 0, -1, 1, 0) (1, 0, 1, -1, 0, 0, 0) (0, 0, 0, 0, 0, 0, 2)
		2	8	(0, -1, 1, -1, 1, 1, 0) (1, 0, 0, 0, -1, 1, 0)
		3	5	(0, -1, 0, 1, 0, 0, 0) (1, 0, 0, -1, 1, 1, 0)
		4	4	(1, -1, 1, 0, 0, 0, 0)
		5	1	(0, 1, 0, 0, 0, 0, 0)
17.		1	9	(1, 0, 0, 0, -1, 1, 0) (0, 0, 0, 0, 0, 0, 2)

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Nilpotent orbits in type EVI (continued)				
Orbit	$K_{\mathbb{C}}$ diagram	i	$\dim \mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$	Highest weights of $\mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$
18.		3	6	(0, -1, 0, 1, 0, 0)
		4	8	(1, -1, 1, 0, 0, 0)
		5	1	(0, 1, 0, 0, 0, 0)
		1	9	(0, 0, 0, -1, 2, 0, 0) (0, -1, 1, 0, -1, 1, 0) (1, 0, 1, -1, 0, 0, 0)
		2	8	(0, -1, 1, -1, 1, 1, 0) (1, 0, 0, 0, -1, 1, 0)
19.		3	6	(0, -1, 0, 1, 0, 0, 0) (1, 0, 0, -1, 1, 1, 0) (0, 0, 0, 0, 0, 0, 2)
		4	4	(1, -1, 1, 0, 0, 0, 0)
		5	1	(0, 1, 0, 0, 0, 0, 0)
		4	15	(0, 1, 0, 0, 0, 0, 0)
		2	16	(1, 0, 0, -1, 1, 1, 0)
20.		4	7	(0, 1, 0, 0, 0, 0, 0) (0, 0, 0, 0, 0, 0, 2)
		2	15	(0, -1, 0, 1, 0, 0, 0) (1, 0, 0, 0, -1, 1, 0) (0, 0, 0, 0, 0, 0, 2)
		4	8	(1, -1, 1, 0, 0, 0, 0)
		6	1	(0, 1, 0, 0, 0, 0, 0)
		4	15	(0, 1, 0, 0, 0, 0, 0)
22.		8	1	(0, 0, 0, 0, 0, 0, 2)
		2	8	(1, 0, 0, 0, -1, 1, 0)
		4	7	(0, -1, 0, 1, 0, 0, 0) (0, 0, 0, 0, 0, 0, 2)
		6	8	(1, -1, 1, 0, 0, 0, 0)
		8	1	(0, 1, 0, 0, 0, 0, 0)
23.		2	8	(1, 0, 0, 0, -1, 1, 0)
		4	7	(0, -1, 0, 1, 0, 0, 0) (0, 0, 0, 0, 0, 0, 2)
		6	8	(1, -1, 1, 0, 0, 0, 0)
		8	1	(0, 1, 0, 0, 0, 0, 0)
		2	8	(0, 0, -1, 1, -1, 1, 0) (0, 0, -1, 1, 1, -1, 0) (-1, 1, 0, 1, -1, -1, 0)
24.		3	6	(1, 1, -1, 0, 0, 0, 0) (0, 0, -1, 0, 1, 1, 0) (-1, 1, 0, 0, -1, 1, 0) (-1, 1, 0, 0, 1, -1, 0) (0, 0, 0, 0, 0, 0, 2)
		1	8	(1, 0, 0, 1, -1, -1, 0) (-1, 1, -1, 1, 0, 0, 0)
		2	8	(1, 0, 0, 0, -1, 1, 0) (1, 0, 0, 0, 1, -1, 0) (-1, 0, 1, 0, 0, 0, 0)
		4	3	(1, 0, 0, 0, 0, 0, 0)
				(continued on next page)

Nilpotent orbits in type EVI (continued)				
Orbit	$K_{\mathbb{C}}$ diagram	i	$\dim \mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$	Highest weights of $\mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$
25.	 $0 \quad 4 \quad 0 \quad 0 \quad 0 \quad 4$	5	2	(1, 0, -1, 1, 0, 0, 0)
		6	2	(0, 1, 0, 0, 0, 0, 0)
26.	 $0 \quad 2 \quad 0 \quad 2 \quad 0 \quad 0$	4	17	(1, -1, 1, 0, 0, 0, 0) (0, 0, 0, 0, 0, 0, 2)
		8	1	(0, 1, 0, 0, 0, 0, 0)
		2	12	(1, 0, 1, -1, 0, 0, 0) (0, -1, 1, -1, 1, 1, 0)
		4	9	(0, -1, 0, 1, 0, 0, 0) (1, 0, 0, -1, 1, 1, 0)
27.	 $1 \quad 1 \quad 1 \quad 1 \quad 0 \quad 1$	6	7	(0, 0, 0, -1, 2, 0, 0) (0, -1, 2, -1, 0, 0, 0) (-1, 2, -1, 0, 0, 0, 0) (2, -1, 0, 0, 0, 0, 0) (0, 0, -1, 1, -1, 1, 0) (0, 0, 0, 0, 0, 2)
		2	6	(-1, 1, 1, -1, 0, 0, 0) (1, 1, -1, 0, 0, 0, 0) (0, 0, -1, 0, 1, 1, 0) (0, -1, 1, 0, -1, 1, 0)
		3	5	(1, 0, 1, -1, 0, 0, 0) (0, -1, 1, -1, 1, 1, 0) (-1, 1, 0, 0, -1, 1, 0)
		4	5	(0, -1, 0, 1, 0, 0, 0) (-1, 1, 0, -1, 1, 1, 0) (1, 0, 0, 0, -1, 1, 0)
		5	3	(-1, 1, -1, 1, 0, 0, 0) (1, 0, 0, -1, 1, 1, 0)
		6	2	(-1, 0, 1, 0, 0, 0, 0) (1, 0, -1, 1, 0, 0, 0)
		7	1	(1, -1, 1, 0, 0, 0, 0)
		8	1	(0, 1, 0, 0, 0, 0, 0)
28.	 $2 \quad 0 \quad 1 \quad 0 \quad 1 \quad 4$	1	6	(0, 0, -1, 1, -1, 1, 0) (-1, 1, 0, 1, -1, -1, 0)
		2	4	(1, 1, -1, 0, 0, 0, 0) (-1, 1, 0, 0, -1, 1, 0)
		3	4	(0, 0, -1, 1, 1, -1, 0) (1, 0, 0, 1, -1, -1, 0)
		4	5	(0, 0, -1, 0, 1, 1, 0) (-1, 1, 0, 0, 1, -1, 0) (1, 0, 0, 0, -1, 1, 0) (0, 0, 0, 0, 0, 0, 2)
		5	4	(-1, 1, -1, 1, 0, 0, 0)
		6	2	(1, 0, 0, 0, 1, -1, 0) (-1, 0, 1, 0, 0, 0, 0)
		7	2	(1, 0, -1, 1, 0, 0, 0)
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Nilpotent orbits in type EVI (continued)				
Orbit	$K_{\mathbb{C}}$ diagram	i	$\dim \mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$	Highest weights of $\mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$
29.	 $\begin{array}{cccccc} & & 0 & & & \\ \circ & - & \circ & - & \circ & - & \circ & - & \circ & \circ \\ 0 & & 0 & & 4 & & 0 & & 0 & 0 \end{array}$	4	18	(1, 0, -1, 1, 0, 0, 0)
		8	3	(0, 1, 0, 0, 0, 0, 0)
30.	 $\begin{array}{ccccccc} & & 1 & & & & \\ \circ & - & \circ & - & \circ & - & \circ & - & \circ & \circ \\ 0 & & 1 & & 0 & & 3 & & 0 & 0 \end{array}$	1	5	(0, 0, 0, -1, 2, 0, 0) (1, 0, 1, -1, 0, 0, 0)
		3	5	(0, -1, 1, 0, -1, 1, 0) (0, 0, 0, 0, 0, 2)
		4	8	(0, -1, 1, -1, 1, 1, 0) (1, 0, 0, 0, -1, 1, 0)
		5	4	(1, 0, 0, -1, 1, 1, 0)
		7	1	(0, -1, 0, 1, 0, 0, 0)
		8	4	(1, -1, 1, 0, 0, 0, 0)
		9	1	(0, 1, 0, 0, 0, 0, 0)
31.	 $\begin{array}{ccccccc} & & 2 & & & & \\ \circ & - & \circ & - & \circ & - & \circ & - & \circ & \circ \\ 0 & & 2 & & 0 & & 2 & & 0 & 2 \end{array}$	2	10	(0, 0, 0, -1, 2, 0, 0) (0, -1, 1, 0, -1, 1, 0) (1, 0, 1, -1, 0, 0, 0) (0, 0, 0, 0, 0, 2)
		4	8	(0, -1, 1, -1, 1, 1, 0) (1, 0, 0, 0, -1, 1, 0)
		6	5	(0, -1, 0, 1, 0, 0, 0) (1, 0, 0, -1, 1, 1, 0)
		8	4	(1, -1, 1, 0, 0, 0, 0)
		10	1	(0, 1, 0, 0, 0, 0, 0)
32.	 $\begin{array}{ccccccc} & & 0 & & & & \\ \circ & - & \circ & - & \circ & - & \circ & - & \circ & \circ \\ 0 & & 0 & & 0 & & 4 & & 0 & 0 \end{array}$	4	17	(1, 0, 0, -1, 1, 1, 0) (0, 0, 0, 0, 0, 2)
		8	6	(0, 1, 0, 0, 0, 0, 0)
33.	 $\begin{array}{ccccccc} & & 4 & & & & \\ \circ & - & \circ & - & \circ & - & \circ & - & \circ & \circ \\ 0 & & 2 & & 0 & & 2 & & 0 & 0 \end{array}$	2	8	(0, -1, 1, 0, -1, 1, 0) (1, 0, 1, -1, 0, 0, 0)
		4	6	(0, 0, 0, -1, 2, 0, 0) (1, 0, 0, 0, -1, 1, 0) (0, 0, 0, 0, 0, 2)
		6	4	(0, -1, 1, -1, 1, 1, 0)
		8	5	(0, -1, 0, 1, 0, 0, 0) (1, 0, 0, -1, 1, 1, 0)
		10	4	(1, -1, 1, 0, 0, 0, 0)
		12	1	(0, 1, 0, 0, 0, 0, 0)
34.	 $\begin{array}{ccccccc} & & 4 & & & & \\ \circ & - & \circ & - & \circ & - & \circ & - & \circ & \circ \\ 0 & & 4 & & 0 & & 0 & & 0 & 8 \end{array}$	4	14	(0, -1, 0, 1, 0, 0, 0) (1, 0, 0, 0, -1, 1, 0)
		8	9	(1, -1, 1, 0, 0, 0, 0) (0, 0, 0, 0, 0, 0, 2)
		12	1	(0, 1, 0, 0, 0, 0, 0)
35.	 $\begin{array}{ccccccc} & & 0 & & & & \\ \circ & - & \circ & - & \circ & - & \circ & - & \circ & \circ \\ 4 & & 0 & & 0 & & 4 & & 0 & 0 \end{array}$	4	15	(1, 0, 1, -1, 0, 0, 0) (-1, 1, 0, -1, 1, 1, 0)
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Nilpotent orbits in type EVI (continued)				
Orbit	$K_{\mathbb{C}}$ diagram	i	$\dim \mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$	Highest weights of $\mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$
36.		8	7	(1, 0, 0, -1, 1, 1, 0) (-1, 0, 1, 0, 0, 0, 0)
		12	3	(0, 1, 0, 0, 0, 0, 0)
		4	13	(1, 0, 1, -1, 0, 0, 0) (0, -1, 1, -1, 1, 1, 0) (0, 0, 0, 0, 0, 0, 2)
		8	9	(0, -1, 0, 1, 0, 0, 0) (1, 0, 0, -1, 1, 1, 0)
37.		12	4	(1, -1, 1, 0, 0, 0, 0)
		16	1	(0, 1, 0, 0, 0, 0, 0)
		4	9	(0, 0, 0, -1, 2, 0, 0) (0, -1, 1, 0, -1, 1, 0) (1, 0, 1, -1, 0, 0, 0)
		8	9	(0, -1, 1, -1, 1, 1, 0) (1, 0, 0, 0, -1, 1, 0) (0, 0, 0, 0, 0, 0, 2)
		12	5	(0, -1, 0, 1, 0, 0, 0) (1, 0, 0, -1, 1, 1, 0)
		16	4	(1, -1, 1, 0, 0, 0, 0)
		20	1	(0, 1, 0, 0, 0, 0, 0)

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