PREHOMOGENEOUS SPACES ASSOCIATED WITH NILPOTENT ORBITS IN TYPE *FI*

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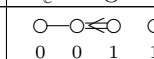
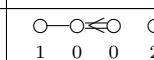
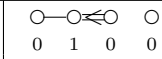
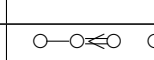
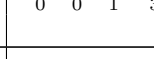
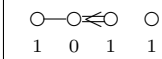
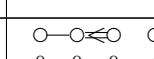
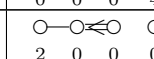
Nilpotent orbits in type *FI*				
Orbits	$K_{\mathbb{C}}$ Diagram	i	$\dim \mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$	Highest weights of $\mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$
1		1	7	$(2,0,0,0)$ $(0,0,0,2)$
2		1	4	$(0,1,0,0)$
		2	2	$(2,0,0,0)$ $(0,0,0,2)$
3		1	4	$(1,-1,1,0)$
		2	3	$(2,0,0,0)$
4		1	6	$(2,0,0,0)$
		3	1	$(0,0,0,2)$
5		1	6	$(1,1,-1,0)$ $(-2,2,0,0)$ $(0,0,0,2)$
		2	2	$(0,1,0,0)$
		3	1	$(2,0,0,0)$
6		4	1	$(0,0,0,2)$
7		2	4	$(0,1,0,0)$
		4	1	$(2,0,0,0)$
8		2	7	$(2,0,0,0)$ $(0,0,0,2)$
9		2	4	$(1,-1,1,0)$
		4	3	$(2,0,0,0)$
10		1	3	$(2,-1,0,0)$ $(-1,0,1,0)$
		2	4	$(-2,2,0,0)$ $(1,-1,1,0)$ $(0,0,0,2)$
		3	1	$(0,1,0,0)$
		4	1	$(2,0,0,0)$

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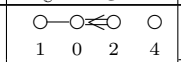
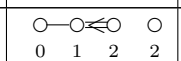
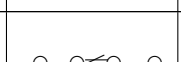
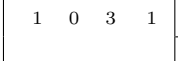
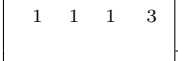
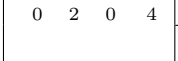
Nilpotent orbits in type *FI* (continued)				
Orbits	$K_{\mathbb{C}}$ Diagram	i	$\dim \mathfrak{g}^i_{\mathbb{C}} \cap \mathfrak{k}_{\mathbb{C}}$	Highest weights of $\mathfrak{g}^i_{\mathbb{C}} \cap \mathfrak{k}_{\mathbb{C}}$
11		1	2	$(1,1,-1,0)$
		2	3	$(-2,2,0,0)$
		3	2	$(0,1,0,0)$
		4	2	$(2,0,0,0)$ $(0,0,0,2)$
12		1	2	$(1,1,-1,0)$
		2	2	$(0,-2,2,0)$ $(0,0,0,2)$
		3	2	$(1,-1,1,0)$
		4	3	$(2,0,0,0)$
13		1	4	$(0,-2,2,0)$ $(-1,2,-1,0)$ $(2,-1,0,0)$ $(0,0,0,2)$
		2	2	$(-1,0,1,0)$ $(1,1,-1,0)$
		3	2	$(-2,2,0,0)$ $(1,-1,1,0)$
		4	1	$(0,1,0,0)$
		5	1	$(2,0,0,0)$
14		1	3	$(1,1,-1,0)$ $(0,0,0,2)$
		3	3	$(-2,2,0,0)$
		4	2	$(0,1,0,0)$
		5	1	$(2,0,0,0)$
15		1	3	$(0,-2,2,0)$ $(-1,2,-1,0)$ $(2,-1,0,0)$
		2	2	$(-1,0,1,0)$ $(1,1,-1,0)$
		3	3	$(-2,2,0,0)$ $(1,-1,1,0)$ $(0,0,0,2)$
		4	1	$(0,1,0,0)$
		5	1	$(2,0,0,0)$
16		4	6	$(2,0,0,0)$
17		2	4	$(1,-1,1,0)$
		4	4	$(2,0,0,0)$ $(0,0,0,2)$
18		2	6	$(1,1,-1,0)$ $(-2,2,0,0)$ $(0,0,0,2)$

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Nilpotent orbits in type $\boldsymbol{FI}$ (continued)				
Orbits	$K_{\mathbb{C}}$ Diagram	i	$\dim \mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$	Highest weights of $\mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$
		4	2	$(0,1,0,0)$
		6	1	$(2,0,0,0)$
19		4	6	$(2,0,0,0)$
		8	1	$(0,0,0,2)$
20		2	2	$(1,1,-1,0)$
		4	4	$(-2,2,0,0)$ $(0,0,0,2)$
		6	2	$(0,1,0,0)$
		8	1	$(2,0,0,0)$
21		1	2	$(0,-2,2,0)$ $(2,-1,0,0)$
		3	2	$(-1,2,-1,0)$ $(0,0,0,2)$
		4	2	$(-1,0,1,0)$ $(1,1,-1,0)$
		5	1	$(1,-1,1,0)$
		7	1	$(-2,2,0,0)$
		8	1	$(0,1,0,0)$
		9	1	$(2,0,0,0)$
22		4	5	$(1,-1,1,0)$ $(0,0,0,2)$
		8	3	$(2,0,0,0)$
23		2	4	$(0,-2,2,0)$ $(-1,2,-1,0)$ $(2,-1,0,0)$ $(0,0,0,2)$
		4	2	$(-1,0,1,0)$ $(1,1,-1,0)$
		6	2	$(-2,2,0,0)$ $(1,-1,1,0)$
		8	1	$(0,1,0,0)$
		10	1	$(2,0,0,0)$
24		2	2	$(-1,2,-1,0)$ $(2,-1,0,0)$
		4	3	$(0,-2,2,0)$ $(1,1,-1,0)$ $(0,0,0,2)$
		6	1	$(-1,0,1,0)$
		8	2	$(-2,2,0,0)$ $(1,-1,1,0)$
		10	1	$(0,1,0,0)$
		12	1	$(2,0,0,0)$
25		4	5	$(1,1,-1,0)$ $(-2,2,0,0)$

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Nilpotent orbits in type *FI* (continued)				
Orbits	$K_{\mathbb{C}}$ Diagram	i	$\dim \mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$	Highest weights of $\mathfrak{g}_{\mathbb{C}}^i \cap \mathfrak{k}_{\mathbb{C}}$
		8	3	$(0,1,0,0)$ $(0,0,0,2)$
		12	1	$(2,0,0,0)$
26		4	3	$(0,-2,2,0)$ $(-1,2,-1,0)$ $(2,-1,0,0)$
		8	3	$(-1,0,1,0)$ $(1,1,-1,0)$ $(0,0,0,2)$
		12	2	$(-2,2,0,0)$ $(1,-1,1,0)$
		16	1	$(0,1,0,0)$
		20	1	$(2,0,0,0)$

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