

FORMS OF THE LINEAR FUNCTION GENERAL EQUATION

$$y = mx + b$$

Slope-intercept form.

$$y - y_1 = m(x - x_1)$$

Point-slope form.

(x_1, y_1) is a point on the graph.

$$Ax + By = C$$

" $Ax + By = C$ " form.

A , B , and C stand for constants.

Objective:

Given an equation in point-slope form, plot the graph quickly, and transform it to the other two forms.

EXAMPLE

$$\text{If } y - 5 = -\frac{3}{2}(x + 1),$$

$(y - k) = m(x - h)$ Point-slope form
point = (h, k)

- Plot the graph quickly.
- Transform the equation to slope-intercept form.
- Transform the equation to $Ax + By = C$ form, where A , B , and C stand for integer constants.

Solution

- From the equation, the slope is $-\frac{3}{2}$. A point on the graph is $(-1, 5)$ because substituting 5 for y makes the left member 0 and substituting -1 for x makes the right member 0. The graph is shown in Figure 3-3.

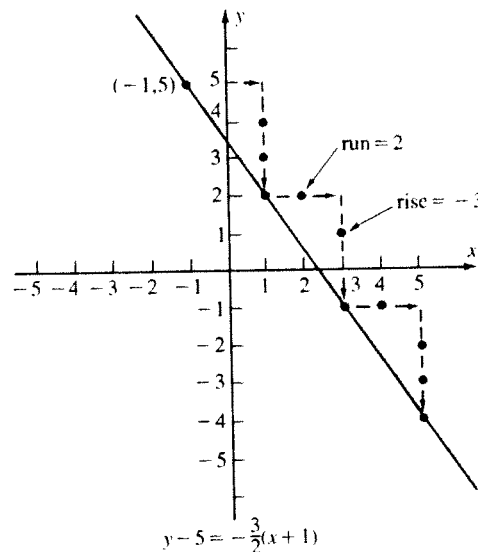


Figure 3-3

- The equation can be transformed to slope-intercept form by distributing the $-\frac{3}{2}$, then adding 5 to each member.

$$y - 5 = -\frac{3}{2}(x + 1),$$

$$y - 5 = -1.5x - 1.5$$

$$\underline{\underline{y = -1.5x + 3.5}}$$

- Starting with the answer in part (b), you can add $1.5x$ to each member, then multiply by 2 to make each coefficient an integer.

$$1.5x + y = 3.5$$

$$\underline{\underline{3x + 2y = 7}}$$

EXAMPLE
FOR
HW 4-B

For Problems 1 through 20, plot the graph neatly on graph paper. Use the slope and y-intercept, where possible.

PART
A

- | | |
|----------------------------|----------------------------|
| 1. $y = \frac{3}{5}x + 3$ | 2. $y = \frac{5}{2}x - 1$ |
| 3. $y = -\frac{3}{2}x - 4$ | 4. $y = -\frac{1}{4}x + 3$ |
| 5. $y = 2x - 5$ | 6. $y = 3x - 2$ |
| 7. $y = -3x + 1$ | 8. $y = -2x + 6$ |
| 9. $7x + 2y = 10$ | 10. $3x + 5y = 10$ |
| 11. $x - 4y = 12$ | 12. $2x - 5y = 15$ |
| 13. $y = 3x$ | 14. $y = -2x$ |
| 15. $y = 3$ | 16. $y = -5$ |

HW 4

For Problems 1 through 10,

PART
B

- Plot the graph, showing clearly the point and slope that appear in the equation.
- Transform the equation to slope-intercept form.
- Transform the equation to $Ax + By = C$ form, where A , B , and C are all integers.

- | | |
|----------------------------------|----------------------------------|
| 1. $y - 2 = \frac{3}{5}(x - 1)$ | 2. $y - 3 = \frac{2}{5}(x - 6)$ |
| 3. $y + 4 = \frac{7}{2}(x - 3)$ | 4. $y + 1 = \frac{7}{3}(x - 4)$ |
| 5. $y - 6 = -\frac{1}{4}(x + 2)$ | 6. $y - 2 = -\frac{1}{2}(x + 5)$ |
| 7. $y + 1 = -2(x + 4)$ | 8. $y + 6 = -3(x + 2)$ |
| 9. $y = \frac{1}{3}(x - 12)$ | 10. $y - 5 = \frac{2}{5}x$ |