

Preliminary Review Class Worksheet

(see web for expanded versions: 0/0-backgroundexamples.pdf and 0/2/expproblems.pdf)
Math 130 Kovitz

1. Solve for x : $2x^2 - x + \frac{1}{9} = 0$.
2. Simplify: $(x^2 - 1) - (x - 1)^2$.
3. Simplify to a single fraction: $\frac{x - 1}{x + 1} - \frac{4}{x^2 - 1}$.
4. If possible, simplify: $\sqrt{x^2 - 2x + 1}$.
Be careful! The first idea that comes to mind may not be correct for all possible x .
5. (a) Divide 4 by $-1/4$.
(b) Simplify $8 \div \frac{1}{3} + \frac{2}{3}$.
6. Subtract. $(5x^2 - 8x + 1) - (8x^2 - 2x + 6)$
7. Multiply. $-3a^2(a^2 - 4a + 5)$
8. Multiply:
 - (a) $(6x - 1)(2x + 5)$.
 - (b) $(2a - 7)^2 - 30$.
 - (c) $3(x - 1/4)^2 + 2$.
9. Divide.
$$\frac{72x^3 - 32x^2 + 8x}{8x}$$

10. Factor.
 - (a) $3x^2 - 75$
 - (b) $9x^2 - 30x + 25$
 - (c) $x^2 + x - 12$
 - (d) $12x^2 - 17x - 40$
11. True or false?
 - (a) $(-2)(-3) = -(2)(3)$
 - (b) $\frac{-5}{-6} = -\left(\frac{5}{6}\right)$
12. (a) Simplify this expression so that it stays in factored form without a leading minus sign.
$$-[(2 - \sqrt{2})(3 - \sqrt{3})]$$

- (b) Solve for x .
$$-x = \frac{\sqrt{6} - \sqrt{3}}{\sqrt{2} - \sqrt{5}}$$

13. Simplify.
 - (a) $\frac{ab - b^2}{5ab - 5a^2}$
 - (b) $\frac{x}{x - 3} - \frac{x - 7}{x - 1} - \frac{1}{2}$
 - (c) $\frac{a^2 - 5}{a - b} + \frac{b^2 - 5}{b - a}$

14. Solve for x . $\frac{20}{x} + \frac{15}{x-7} = 7$.
15. Solve for d . $A = \frac{1}{2}h(c-d)$.
16. Solve for x . (real number solutions only)
- $x^2 - 22x = 11$
 - $x^2 - x + 1 = 0$
 - $5x^2 - x - 4 = 0$
 - $(x - 4139)^2 = 161^2$.
17. Simplify, if you can: $\sqrt{a^2 + b^2}$.

The remaining problems review rules of exponents.

18. Simplify: $4^{-2}, 4^{1/2}, 4^{-3/2}, 4^{-2/3}, 256^{-3/4}, 243^{-6}, 144^{1/4} \cdot 144^{3/4}, 16^{3/4} + 16^{1/4}$.

19. Simplify: $\left(\frac{1}{2}\right)^3 (-2)^3, \frac{3^2}{3^0}, \frac{(-2)^5}{(-2)^2}$.

20. True or False?

- $4^{8/3} \cdot 4^{4/3} = 256$.
- $4^{8/3} \div 4^{2/3} = 16$.
- $8^{5/6} \div 8^{-1/6} = 4$.
- $(4^{4/3})^3 = (\sqrt[4]{4})^{16}$.
- $4^{3 \times 7} = 4^3 + 4^7$.
- $4^{3 \times 7} = 4^3 \cdot 4^7$.
- $4^{-3/4} = \sqrt{2}/4$.
- $\left(\frac{4}{\sqrt[4]{4}}\right)^4 = 64$.
- $8^{4/3} + 8^{2/3} = 24$.

21. Let $y = 16^x$

- Find y when $x =: \frac{1}{4}, -1, 2$.
- For which x is y equal to: $4, \frac{1}{16}, \frac{1}{\sqrt{2}}, -256$?

22. Simplify: $\sqrt{x} \cdot \sqrt{x}$.

23. Rewrite using positive exponents and then simplify: $x^{-2} + y^{-2}$.

24. Solve for x :

$$8^x = \frac{1}{\sqrt[3]{4}}$$

25. Solve for c and x .

$$cx^2 = 0.5$$

$$cx^5 = 32$$

26. Write in a simpler form: $(\sqrt[3]{6})^{3/2}$.